

160(b) : Reduction of the General Formula to the Usual Compton Effect Formula.

The general formula is:

$$x_2 = \frac{\omega\omega'}{\omega - \omega'} - \left( \frac{x_1^2 + (\omega^2 - x_1^2)^{1/2} (\omega'^2 - x_1^2)^{1/2} \cos\theta}{\omega - \omega'} \right) \quad - (1)$$

where  $x_2 = \frac{m_2 c^2}{h}$ ,  $x_1 = \frac{m_1 c^2}{h}$ . - (2)

This reduces as follows to the usual formula if:

$$x_1 \rightarrow 0. \quad - (3)$$

Then:  $x_2 = \frac{\omega\omega'}{\omega - \omega'} (1 - \cos\theta) \quad - (4)$

i.e.  $\omega - \omega' = \frac{\omega\omega'}{x_2} (1 - \cos\theta) \quad - (5)$

or  $\frac{1}{\omega'} - \frac{1}{\omega} = \frac{h}{m_2 c^2} (1 - \cos\theta) \quad - (6)$

Finally we  $\omega = 2\pi f$ ,  $f\lambda = c$ ,  $\omega = \frac{2\pi c}{\lambda} \quad - (7)$

to get:  $\lambda' - \lambda = \frac{h}{m_2 c} (1 - \cos\theta) \quad - (8)$

which is the usual formula, Q.E.D. The usual formula is true only if  $m_1 \rightarrow 0$ . - (9)

In the case of the electron this is not true, so the theory fails.