

# 255(9): Suggested Interpretation of the Inhomogeneous Field Equations

In vector notation these are:

$$\underline{\nabla} \cdot \underline{E}^a = \rho^a / \epsilon_0 \quad - (1)$$

$$\underline{\nabla} \times \underline{B}^a - \frac{1}{c^2} \frac{d\underline{E}^a}{dt} = \mu_0 \underline{J}^a \quad - (2)$$

The left hand side refer to the electromagnetic field,  
and the right hand side to material matter. On the left  
hand side:

$$\underline{E}^a = c A^{(0)} \underline{T}^a (\text{orbital}) \quad - (3)$$

$$\underline{B}^a = A^{(0)} \underline{T}^a (\text{spin}) \quad - (4)$$

in S.I. units. The scaling constant  $A^{(0)}$  refers  
to the field.

On the right hand side:

$$\rho^a = \epsilon_0 c A_{\text{matter}}^{(0)} \left( \underline{\omega}^a_b \cdot \underline{T}^b (\text{orbital}) - \underline{v}^b \cdot \underline{R}^a_b (\text{orbital}) \right) \quad - (5)$$

$$\underline{J}^a = \epsilon_0 c^2 A_{\text{matter}}^{(0)} \left( \underline{\omega}^a_b \underline{T}^b (\text{orbital}) - \underline{v}^b \cdot \underline{R}^a_b (\text{orbital}) \right. \\ \left. + \underline{\omega}^a_b \times \underline{T}^b (\text{spin}) - \underline{v}^b \times \underline{R}^a_b (\text{spin}) \right) \quad - (6)$$

where  $A_{\text{matter}}^{(0)}$  refers to material matter.

2) This is the way in which the EEF theory has been developed to date. The computational problem is reduced to eqn. (1) and (2), with all the terms in eqs. (5) and (6) grouped together. If the electro-magnetic field interacts with the vacuum then  $A^{(0)}$  matter is replaced with  $A^{(0)}$  vacuum, the vacuum potential (orbital).

Therefore

$$\underline{E}^a(\text{matter}) = c A_{\text{matter}}^{(0)} \underline{T}^a - (7)$$

$$\underline{A}^a(\text{matter}) = A_{\text{matter}}^{(0)} \underline{q}^a - (8)$$

$$\underline{B}^a(\text{matter}) = A_{\text{matter}}^{(0)} \underline{T}^a(\text{spin}) - (9)$$

$$\underline{E}^a(\text{vacuum}) = A_{\text{vacuum}}^{(0)} \underline{T}^a(\text{orbital}) - (10)$$

$$\underline{A}^a(\text{vacuum}) = A_{\text{vacuum}}^{(0)} \underline{q}^a - (11)$$

$$\underline{B}^a(\text{vacuum}) = A_{\text{vacuum}}^{(0)} \underline{T}^a(\text{spin}) - (12)$$

Spin Currents Resonance Driven by the Vacuum

This is described by:

$$\underline{\nabla} \cdot \underline{E}^a = \rho^a(\text{vacuum}) / \epsilon_0 - (13)$$

$$\underline{\nabla} \times \underline{B}^a - \frac{1}{c^2} \frac{\partial \underline{E}^a}{\partial t} = \mu_0 \underline{\Sigma}^a(\text{vacuum}) - (14)$$

where:

$$3) \quad \underline{E}^a = -c \underline{\nabla} A^a - \frac{\partial A^a}{\partial t} - c \underline{\omega}^a_b A^b + c A^b \underline{\omega}^a_b \quad - (15)$$

$$\underline{B}^a = \underline{\nabla} \times A^a - \underline{\omega}^a_b \times A^b \quad - (16)$$

In the simplest case assume one polarization and  $\underline{A}^a = \underline{0} \quad - (17)$

so only electric fields are present. Then:

$$\underline{E} = - \underline{\nabla} \phi + \underline{\omega} \phi \quad - (18)$$

Assume that  $\underline{\omega}$  is negative:

$$\underline{\omega} = -\omega_x \underline{i} - \omega_y \underline{j} - \omega_z \underline{k} \quad - (19)$$

Then:

$$E_x = - \frac{\partial \phi}{\partial x} - \omega_x \phi$$

$$E_y = - \frac{\partial \phi}{\partial y} - \omega_y \phi \quad - (20)$$

$$E_z = - \frac{\partial \phi}{\partial z} - \omega_z \phi$$

Align it to Z direction. - (21)

$$\frac{\partial}{\partial z} \left( \frac{\partial \phi}{\partial z} + \omega_z \phi \right) = - \frac{\rho(\text{vac})}{\epsilon_0}$$

i.e. 

$$\frac{\partial^2 \phi}{\partial z^2} + \frac{\partial \omega_z}{\partial z} \phi + \omega_z \frac{\partial \phi}{\partial z} = - \frac{\rho(\text{vac})}{\epsilon_0}$$

- (22)

Finally if it is assumed that:

$$\frac{\rho(\text{vac})}{\epsilon_0} = \frac{\rho_0}{\epsilon_0} \cos(\kappa_0 z)$$

$$= -\frac{\rho_0}{\epsilon_0} \cos(\kappa_0 z) \quad - (23)$$

Then a damped Euler Bernoulli equation is obtained:

$$\frac{\partial^2 \phi}{\partial z^2} + \left( \frac{\partial \omega_2}{\partial z} \right) \phi + \omega_2 \frac{\partial \phi}{\partial z} = \frac{\rho_0(\text{vac})}{\epsilon_0} \cos(\kappa_0 z)$$

- (24)

This can be written as:

$$\boxed{\frac{\partial^2 \phi}{\partial z^2} + \kappa^2 \phi + \beta \frac{\partial \phi}{\partial z} = A \cos(\kappa_0 z)} \quad - (25)$$

where:

$$\kappa^2 = \frac{\partial \omega_2}{\partial z}, \quad A = \frac{\rho_0(\text{vac})}{\epsilon_0}, \quad - (26)$$

$$\beta = \omega_2$$

The S.I. units are:

$$\rho_0(\text{vac}) = \text{C m}^{-3}, \quad \epsilon_0 = \text{J}^{-1} \text{C}^2 \text{m}^{-1},$$

$$A = \text{C m}^{-3} \text{J C}^{-2} \text{m} = \text{J C}^{-1} \text{m}^{-2}$$

$$\phi = \text{C A}^{(0)} = \text{J s C}^{-1} \text{m}^{-1} \text{m} \text{s}^{-1} = \text{J C}^{-1}$$

so eqn (25) is dimensionally correct.

By antisymmetry:

5)

$$\nabla \phi = \underline{\omega} \phi - (27)$$

so in the  $z$  direction:

$$\frac{\partial \phi}{\partial z} = -\omega_z \phi - (28)$$

so eqn. (25) becomes:

$$\frac{\partial^2 \phi}{\partial z^2} + (\kappa^2 + \omega_z^2) \phi = A \cos(\kappa_0 z) - (29)$$

which is an undamped Euler Bernoulli equation:

$$\frac{\partial^2 \phi}{\partial z^2} + \kappa_1^2 \phi = A \cos(\kappa_0 z) - (30)$$

we

$$\kappa_1^2 = \kappa^2 + \omega_z^2 - (31)$$

The solution of eq. (30) is:

$$\phi = \frac{A \cos(\kappa_0 z)}{\kappa_1^2 - \kappa_0^2} - (32)$$

so when

$$\kappa_1^2 = \kappa_0^2 - (33)$$

then

$$\phi \rightarrow \infty - (34)$$

The potential will be infinite because  
infinite, no matter how small the driving term