

15(b): Calculation of the spin correction for Frame Rotation in m Theory.

In m theory, the relevant equations of motion are:

$$V^3 \frac{dr}{dt} = - \frac{1}{m(r)^{1/2}} \frac{MG}{r} \left(\frac{1}{r} + 2r \right) \quad (1)$$

and

$$\frac{dL}{dt} = 0 \quad (2)$$

also

$$L = |\underline{r} \times \underline{p}| = \frac{m r^2}{m(r)} \dot{\phi} \quad (3)$$

The $m(r)$ function of ECE theory is:

$$m(r) = 2 - \exp \left(2 \exp \left(-\frac{r}{R} \right) \right) \quad (4)$$

(UFT 190), and

$$\gamma = \left(m(r) - \frac{v^2}{c^2} \right)^{-1/2} \quad (5)$$

The infinitesimal line element of m theory is:

$$ds^2 = c^2 d\tau^2 = m(r) c^2 dt^2 - \frac{dr^2}{m(r)} - r^2 d\phi^2 \quad (6)$$

As shown in previous UFT papers, eq. (6) produces:

$$\frac{dr}{d\phi} = r^2 \left(\frac{1}{b^2} - m(r) \left(\frac{1}{a^2} + \frac{1}{r^2} \right) \right)^{1/2} \quad (7)$$

also

$$a = \frac{L}{mc}, \quad b = \frac{Lc}{E} \quad (8)$$

Here E is the conserved total energy:

2) $E = \gamma mc^2 - (9)$

and L is the conserved angular momentum (3). It was shown in UFT 108 that a striking orbit is produced by the empirical:

$$n(r) = 1 - \frac{2mG}{c^2 r} - \frac{d}{r^2} - (10)$$

where d is an adjustable parameter.

Now use the frame rotation:

$$\phi' = \phi + \omega_1 t - (11)$$

and

$$\dot{\phi}' = \dot{\phi} + \omega_1 + t \frac{d\omega_1}{dt} - (12)$$

to calculate the spin connection Ω_r .

The frame rotation changes:

$$\gamma^3 = \left(n(r) - \frac{1}{c^2} (\dot{r}^2 + r^2 \dot{\phi}'^2) \right)^{-3/2} - (13)$$

to

$$\gamma'^3 = \left(n(r) - \frac{1}{c^2} (\dot{r}^2 + r^2 \dot{\phi}^2) \right)^{-3/2} - (14)$$

It follows that:

$$\frac{1}{\gamma'^3} - \frac{1}{\gamma^3} = A := \frac{r^2}{c^2} \left(\omega_1 + t \frac{d\omega_1}{dt} \right) \left(\omega_1 + t \frac{d\omega_1}{dt} + 2\omega \right) - (15)$$

and that:

$$\begin{aligned} \gamma^3 (\ddot{r} - r \dot{\phi}'^2) &= -\frac{1}{n(r)^{1/2}} \frac{mG}{r^2} (1 + \gamma^2 A)^{3/2} + \gamma^3 \frac{cA}{r} \\ &:= -\frac{1}{n(r)^{1/2}} \left(\frac{mG}{r^2} - \frac{mG}{r} \Omega_r \right) - (16) \end{aligned}$$

Therefore:

$$\Omega_r = \frac{1}{r n(r)^{1/2}} - \frac{(1 + \gamma^2 A)^{3/2}}{r n(r)^{1/2}} - \frac{\gamma^3 c^2 A}{n(r)} \quad (17)$$

Eq. (17) reduces to the spin correction calculated in UFT414 for:

$$n(r) \rightarrow 1 \quad (18)$$

Q.E.D.

So the orbit can be calculated from eqs. (1) and (2) with a suitable choice of $n(r)$, not only $n(r)$ from Eq. (4). Knowing $n(r)$, the spin correction can be calculated from eq. (17) in terms of ω_1 and $d\omega_1/dt$. It would be interesting to calculate the orbit from eq. (7) using:

$$E = \gamma m c^2, \quad L = \gamma m r^2 \dot{\phi} \quad (19)$$

It would also be interesting to use the empirical function (10)
