

The Force Equations

$$\underline{\nabla} \cdot \underline{F}(\text{spin}) = m_1 m_2 G \underline{j}^0$$

$$\underline{\nabla} \times \underline{F}(\text{orbital}) + \frac{1}{c} \frac{\partial \underline{F}}{\partial t}(\text{spin}) = m_1 m_2 G \underline{j}$$

$$\underline{\nabla} \cdot \underline{F}(\text{orbital}) = m_1 m_2 G \underline{j}^0$$

$$\underline{\nabla} \times \underline{F}(\text{spin}) - \frac{1}{c} \frac{\partial \underline{F}}{\partial t}(\text{orbital}) = m_1 m_2 G \underline{j}$$

$$\underline{F}(\text{orbital}) = m_1 m_2 G \left(R^0_1{}^{01} \underline{i} + R^0_2{}^{02} \underline{j} + R^0_3{}^{03} \underline{k} \right)$$

$$\underline{F}(\text{spin}) = m_1 m_2 G \left(R^2_3{}^{23} \underline{i} + R^1_3{}^{31} \underline{j} + R^1_2{}^{12} \underline{k} \right)$$

These are deduced from the second Cartan structure equation:

$$R^a{}_b = D \wedge \omega^a{}_b$$

and the second Bianchi identity:

$$D \wedge R^a{}_b := 0$$

for a spherically symmetric spacetime.