

$$\mu = 0 \quad - (14)$$

Eqs. (7) to (12) simplify to:

$$\omega^1_{02} = -\omega^2_{01} = \frac{\kappa}{2} \nabla_0^0, \quad - (15)$$

$$\omega^1_{03} = -\omega^3_{01} = \frac{\kappa}{2} \nabla_0^0, \quad - (16)$$

$$\omega^2_{03} = -\omega^3_{02} = \frac{\kappa}{2} \nabla_0^0. \quad - (17)$$

So for electro-statics there is only one independent spin connection element.

The scalar potential ϕ_0^a must be the same scalar in all frames of reference. It

follows that:

$$\phi_0^a = \phi^{(0)} \begin{bmatrix} 1 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 \\ 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}, \quad \nabla_0^a = \begin{bmatrix} 1 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 \\ 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}. \quad - (18)$$

The product of ω^a_b and ϕ^b must be $(i = 1, 2, 3)$:

$$\begin{aligned} \omega^a_{ib} \phi^b &= \omega^a_{i1} \phi^1 + \omega^a_{i2} \phi^2 + \omega^a_{i3} \phi^3 \\ &= \phi^{(0)} (\omega^a_{i1} + \omega^a_{i2} + \omega^a_{i3}). \quad - (19) \end{aligned}$$

From Eq. (10) it is seen that:

$$a = 1, 2, 3. \quad - (20)$$

Thus:

$$\underline{E}^1 = -\underline{\nabla} \phi - \underline{\kappa} \phi, \quad - (21)$$

$$\underline{E}_1 = \underline{E}^1, \quad - (21a)$$